Performance Assessment of the World Wide Lightning Location Network (WWLLN),
Using the Los Alamos Sferic Array (LASA) as Ground Truth

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(Manuscript received 11 June 2005, in final form 5 December 2005)

ABSTRACT

The World Wide Lighting Location Network (WWLLN) locates lightning globally, using sparsely distributed very low frequency (VLF) detection stations. Due to WWLLN's detection at VLF (in this case ~10 kHz), the lightning signals from strong strokes can propagate up to ~10^4 km to WWLLN sensors and still be suitable for triggering a station. A systematic evaluation of the performance of WWLLN is undertaken, using a higher-frequency (0–500 kHz) detection array [the Los Alamos Sferic Array (LASA)] as a ground truth during an entire thunderstorm season in a geographically confined case study in Florida. It is found that (a) WWLLN stroke-detection efficiency rises sharply to several percent as the estimated lightning current amplitude surpasses ~30 kA; (b) WWLLN spatial accuracy is around 15 km, good enough to resolve convective-storm cells within a larger storm complex; (c) WWLLN is able to detect intracloud and cloud-to-ground discharges with comparable efficiency, as long as the current is comparable; (d) WWLLN detects lightning-producing storms with high efficiency in every 3-h epoch; thus, WWLLN can be useful for locating deep convection for weather forecasting on 3-h update cycles; and (e) WWLLN detects a stroke count in each storm that is weakly proportional to the stroke count detected by LASA. Thus, to the extent that lightning rate can serve as a statistical proxy for rainfall, WWLLN may eventually provide rainfall-proxy data to be assimilated in 3-h forecast update cycles.

1. Introduction

It is now widely recognized that real-time remote sensing of lightning can assist in identification and monitoring of severe convective weather. Different lightning remote sensing systems have complementary levels of detail, range, and application. The finest lightning detail, but also the most restricted geographical range, is provided by very high frequency (VHF) lightning-mapping arrays (LMAs), amongst which the New Mexico Institute of Mining and Technology's LMA has been the best-known system (Rison et al. 1999; Thomas et al. 2000, 2001). Affording less detail, but potentially unlimited geographical range, is space-based optical lightning detection from geostationary orbit (Christian et al. 1989). Toward this end, the OTD and LIS lightning imagers from low-earth-orbit (Boccippio et al. 2000a,b, 1999; Christian et al. 1999a,b) have recently demonstrated that satellite optical imaging can provide a monitor of “total lightning,” that is, both cloud-to-ground (CG) and intracloud (IC) discharges, with high detection efficiency (DE) and global coverage.

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For ground-based monitoring of CG activity, low-frequency (LF) detection arrays, exemplified by the U.S. National Lightning Detection Network (NLDN), give excellent coverage of almost all continental storms, which account for most global lightning (Cummins et al. 1998). NLDN and similar systems provide not only accurate location (<1 km errors) and high DE (>90%), but also an estimate of discharge vertical-current amplitude and polarity. NLDN-like systems now operate on parts of most continents. These systems provide operationally useful real-time information for weather-hazard mitigation, forest-fire response, and electric-grid emergency response. NLDN and similar systems have also provided a wealth of scientific information (Carey et al. 2003; Lyons et al. 1998; Orville 1994; Orville et al. 2001) and precise benchmarks against which to calibrate the performance of other systems (Jacobson et al. 2000; Lay et al. 2004; Smith et al. 2002).

The Los Alamos Sferic Array (LASA) is a variation of the NLDN-style low-frequency array. LASA has been implemented (Smith et al. 2002) for specific, geographically delimited campaigns in which it is vital to record and archive the LF waveform from each station participating in a lightning detection/location. LASA has been recently upgraded to allow nearly continuous waveform recording with no “dead time” (Shao et al. 2006). LASA waveform data can be used to identify the lightning process by detailed examination of the waveform, and more importantly, the waveforms for certain IC discharges can be used to retrieve the discharge height above the local ground (Smith et al. 2004). Unlike NLDN, LASA is purely a research facility and is not meant to provide either the geographical coverage, or the up-time reliability, of NLDN.

Providing the least remote sensing detail, but also the greatest range of detection at the lowest cost, is the approach based on detecting vertical-electric-field disturbances in the VLF (3–30 kHz) spectral band. This was begun by the Met Office of the U.K. (Lee 1986a,b) and has more recently provided the basis of other deployed systems including the World Wide Lightning Location Network (WWLLN) (Dowden et al. 2002; Lay et al. 2004; Rodger et al. 2004, 2005).

Long-range (thousands of kilometers) VLF lightning detection can, in principle, provide global coverage, including over remote oceanic regions, for a very modest investment. VLF can do this because its signals are less attenuated than are higher frequencies, such that a VLF array containing on the order of merely 20 stations distributed globally can provide useful coverage of all Tropics and midlatitudes. The penalty is that the wave energy arrives at the sensors via the earth–ionosphere waveguide rather than by line-of-sight (“ground wave”). A VLF system bandwidth is on the order of only 10 kHz, and this already is marginal for retrieving the characteristics of the lightning current waveform even in the case of ground-wave propagation from proximate events. The loss of source characteristics is further worsened by the reflections from the ionosphere and the propagation multipath (earth–ionosphere waveguiding.) The ionospheric interaction spectrally distorts and attenuates the received waveform, so that it is no longer straightforward to infer the vertical-current magnitude or, for that matter, even the vertical-current polarity.

Nonetheless, VLF systems for lightning detection are potentially useful in providing weather data over wide regions, for real-time information in aviation management, for climate studies, and for meteorological forecasting. To perform best, the VLF systems should preferably meet at least three standards:

1) efficient storm detection,
2) proportional stroke detection, and
3) minimal false detections.

The remainder of this article will assess the WWLLN system against these three performance standards.

2. System description

LASA has been a reliable lightning-location array over the Florida region. In addition, LASA records and archives digitized waveforms of the vertical-electric-field transients at each station that participates in a lightning event’s time-difference-of-arrival (TDOA) location of the lightning discharge. The purpose of LASA is to support various lightning projects of the Department of Energy (DOE) and to provide waveforms to lightning researchers. LASA covers only a small fraction of North America, and in the case of this study, the Florida region. LASA is not intended to supplant the NLDN, which provides (at modest cost) reliable (Cummins et al. 1998) stroke- or flash-level lightning location and current estimates over all of North America, at all times.

The LASA system during 2004 operated in its new mode (Stanley et al. 2004), whereby there are no “dead times” between successive recordings. Each record was 1 ms in duration. Thus, during a flash containing multiple discharges, LASA can easily record all successive members of the flash, providing that the stroke vertical-current amplitude exceeds a few kiloamps, and providing that the location is interior to the array. In practice that means lying within a 400-km-radius circle centered on 29°N, 82°W. [This new array center is displaced 0.5°W and 1°N relative to the “old” LASA array cen-
ter, which obtained during 1999–2002 (Jacobson and Heavner 2005).] For records containing more than one lightning pulse, the 2004 upgrade of LASA allows multiple solutions to be tested and, if appropriate, archived. For example, the descending leader prior to a negative CG stroke can create pulses contained within the same 1-ms-duration record that contains the main CG stroke. LASA detects in-cloud discharges of sufficient amplitude. For the purposes of this paper, we will be ultimately focusing on current amplitudes exceeding 30 kA. In practice, practically all of the LASA-detected IC events of this high a current are “narrow bipolar events” (NBEs; Smith et al. 1999, 2002).

Figure 1 shows the WWLLN station locations during the time of this study (summer 2004). The closest WWLLN stations to Florida were in Boston, Massachusetts; Los Alamos, New Mexico; and Seattle, Washington. All of these are separated from the LASA array center by distances that are large compared to the nominal maximum ground-wave distance (≈600 km), beyond which ionospheric pathing may be expected to interfere with, and ultimately (at larger distances) dominate over the ground wave. We required at least five WWLLN stations in each TDOA location solution. All the WWLLN participating stations in this study were detecting the lightning events via earth–ionosphere-waveguide propagation paths. The WWLLN lightning-location solutions were generated using the upgraded “time of group arrival” (TOGA) algorithm at each WWLLN station (Dowden et al. 2002). The WWLLN array station locations and other system parameters can be found online at http://flash.ess.washington.edu/. During the time of this study, there were a maximum of 19 WWLLN stations worldwide.

The quality of WWLL location solutions is governed, in part, by the root-mean-square (rms) residual between the observed and the modeled arrival times of a signal at participating stations. For this study, we used solutions with rms residuals less than 30 μs. Each WWLLN station has a servo-controlled trigger threshold that seeks to keep a constant trigger rate, on the order of five triggers per second. This means that the average intertrigger time will be on the order of 0.2 s. WWLLN stroke detections generally do not occur more than once within a lightning flash. Thus WWLLN stroke detection is effectively also flash detection.

3. Cross-validation campaign

We used data recorded during almost the entire 2004 Florida summer thunderstorm season, including all days from 27 April through 30 September. Both LASA and WWLLN archives were parsed down to those events that occurred within 400 km of 29°N, 82°W. Table 1 lists the numbers of events from WWLLN and LASA in this study zone, both correlated and uncorrelated.

During the check-out and validation of the LASA
system, NLDN data were used as a ground truth against which to evaluate LASA location accuracy (Smith et al. 2002). In a similar spirit, we are now using LASA as a ground truth against which to evaluate WWLLN performance.

Florida is an active lightning region during summer. Its lightning activity tends to occur in airmass thunderstorms that are often regulated by sea-breeze convergence over the Florida Peninsula. The region is particularly poor in positive CG lightning (Carey et al. 2003), so that some aspects of lightning simply cannot be efficiently studied there. Nonetheless, the Florida region is important for characterizing the WWLLN performance statistically, for two reasons. First, Florida is far enough from all circa 2004 WWLLN stations that the signal propagation was necessarily in the earth-ionosphere waveguide. This is in common with the vast majority of the earth surface, given that WWLLN has the ability (or lack thereof) to locate IC activity.

4. WWLLN–LASA time coincidences

We follow well-established practice and measure the distribution of time differences between lightning strokes as measured by LASA and WWLL, conditioned on their respective estimated positions’ being within 100 km of each other. Figure 2a shows the distribution of LASA–WWLL time differences for coincident events. The top panel is for coincidence to all LASA events, the middle is for coincidence to just CG LASA events, and the bottom is for coincidence to just IC LASA events. The distributions’ shoulders (at $\pm 50$ ms) are from other LASA strokes within the same flash. The right shoulder’s greater magnitude, relative to the left shoulder, is due to WWLLN’s tendency to record the first stroke of a flash at a higher efficiency than later ones. On the other hand, the close-in feature in the middle panel, at $-10$ ms, is due to WWLLN-detected leader steps prior to CGs seen by WWLLN. Noted in parentheses in each panel of Fig. 2a is the number of WWLLN events that have a close (±1 ms) LASA coincidence of the respective type; see also Table 1.

There are 75 884 WWLLN events in the study having time-of-arrival residuals $< 30$ $\mu$s and at least five participating stations (see Table 1). Of these, 71 362, or 94%, have close (within ±1 ms) LASA coincidence. That would imply that ~6% of the WWLLN events (a) may be mislocated (by an error $>100$ km), (b) may be formed by a misassociation of station triggers, or (c) may actually be detecting valid events that LASA is missing. We have checked this by graphing locations of the WWLLN events that are not accompanied by coincident LASA events, on a map on which locations of the WWLLN events that are accompanied by coincident LASA events are also graphed, for several example 3-h epochs. We find that both classes of WWLLN events are clustered at the same storm centers. We find that 74 888 WWLLN events are coincident with LASA in a broader time window of 200 ms. This leaves only 996 (=75 884 − 74 888) WWLLN events that are without even a 200-ms LASA coincidence, that is, only 1.7% of the WWLLN events. Therefore, we conclude that most of the 6% of WWLLN events not accompanied by LASA 1-ms coincidences are still valid lightning locations, but of events that were recorded by LASA at the flash level, not at the stroke level.

Thus the Florida LASA array provides for some ground truthing of WWLLN’s ability (or lack thereof) to locate IC activity.

| Table 1. Events during the summer 2004 campaign in the 400-km-radius circle centered on 29°N, 82°W. |
|-----------------|-----------------|-----------------|
| No. of WWLLN events | 75 884          |
| No. of LASA events | 8 923 316       |
| No. of WWLLN events with LASA coincidence within ±1 ms | 71 362          |
| Percent of WWLLN events with LASA coincidence within ±1 ms | 94%             |
| No. of LASA events of type CG | 4 196 004       |
| No. of LASA events of type IC | 4 727 312       |
| No. of WWLLN events with LASA coincidence within ±1 ms of type CG | 52 728*         |
| No. of WWLLN events with LASA coincidence within ±1 ms of type IC | 21 437*         |

* The two entries marked with asterisk sum to 74 165, indicating that (74 165 − 71 362) = 2803 WWLLN events had both CG and IC LASA events within ±1 ms.
WWLLN events with close (within ±1 ms) LASA IC coincidence. These last two numbers exceed the overall number of LASA-coincident WWLLN events (71,362) by 2803, due in part to LASA recording of late leader steps (classified as “IC”) within 1 ms of the stroke, and in part to cloud-level disturbances closely accompanying ground strokes (Jacobson et al. 2000; Suszcynsky et al. 2000, 2001). If we subtract the 2803 WWLLN events that apparently have both CG and IC LASA coincidence, then we still have 21,437 WWLLN events that are due uniquely to IC discharges. This is ∼26% of the WWLLN total events, implying that WWLLN is likely to be able to detect storms that are dominantly IC (Lang et al. 2000), as long as there are NBIs, which alone amongst IC processes tend to produce current amplitudes exceeding 30 kA.

Similar to Fig. 2a, Fig. 2b shows the distribution of time differences LASA–WWLLN for coincident events, but for the subrange ±1 ms and with a narrower bin width (10 μs). Figure 2b shows that the 1/e widths of the time-difference distributions are all on the order of 50 μs.

5. LASA–WWLN spatial coincidences

Figure 3 shows the distributions of eastward (solid curve) and northward (dashed curve) position differences (LASA–WWLN). WWLN solutions in Florida have small (∼couple of kilometers) westward and northward biases. Since WWLN uses distant stations at diverse azimuths having diverse ionospheric-waveguide conditions, it is not surprising that a couple-of-kilometers bias is introduced relative to LSAI location based on purely ground-wave propagation. This bias apparently is not sufficiently large to spoil WWLN’s association of a lightning discharge with the appropriate convective cell. The 1/e width is in the range 15–20 km. This is small enough to ensure that when WWLN locates an event, the event is likely to be associated with the appropriate convective cell in the
overall storm, but is not small enough to indicate meaningfully the placement of the lightning event within that cell.

6. WWLLN stroke-detection efficiency

Figure 4 shows the distributions of LASA-estimated peak vertical current for (a) all LASA events, (b) LASA CG events, and (c) LASA IC events. The dashed curves describe the background LASA population, while the solid curves are for the subset of LASA events having close (within ±1 ms) coincidence with WWLLN events. Figure 4 shows several interesting tendencies. First, the background CG distribution (Fig. 4b, dashed curve) is heavily weighted toward negative CGs, consistent with the negative-CG-dominated climatology of Florida lightning (Carey et al. 2003). Indeed, for practical purposes, we can approximate that there is almost no +CG activity in this study, or at least not enough +CG activity to calibrate the WWLLN detection efficiency for +CG strokes. Second, the IC currents (Fig. 4c, dashed curve) are generally lower than the CG currents, but still extend to several tens of kiloamps. Third, the WWLLN-coincident subset of LASA events systematically occurs at higher current amplitude than does the background distribution of LASA events.

We can estimate a stroke-detection efficiency (stroke DE) for WWLLN by dividing the number of WWLLN-coincident LASA events by the number total background LASA events, separately in each current bin. The results are shown in Fig. 5. We make two inferences. First, the WWLLN DE, at least for −CGs and ICs, is negligible for current magnitudes < 20 kA. Second, the WWLLN DE approaches a few percent for higher (>30 kA) current magnitudes. Apparently, an IC discharge and a −CG discharge are equally detectable for a comparable current. The only reason that more than two-thirds of WWLLN events are nonetheless CG is that (see Fig. 4 above) the current magnitudes of ICs are less than for CGs. Moreover, almost the only ICs with sufficient current to be WWLLN-detectable are NBEs, which have the highest currents of any IC processes (Smith et al. 1999, 2002).

Figure 6 shows similar information as Fig. 5a, but divided into 12-h epochs centered on local (at the LASA centroid) midnight (dashed curve) and local noon (solid curve). The gross changes between midnight- and noon-centered epochs are due to the lossier daytime ionospheric D-region and its effect on long-range VLF propagation of the lightning signal to WWLLN stations.
7. WWLLN storm-detection efficiency

It is clear that WWLLN and similar VLF long-range lightning-detection systems will never provide the focused, detailed view of the interior of a thunderstorm that is provided by various radio-frequency lightning mappers such as LMA. Indeed, VLF systems will never offer the level of detail or detection efficiency even of satellite-based optical imagers. Instead, the products which long-range VLF systems might be able to provide are (a) synoptic location of current convective cells and (b) statistical inference of the rain rate (and hence latent-heat-release rate) to the extent that empirical rain/lightning parameterizations have any skill within the particular meteorological setting. Both of these observational products must be available promptly (though not strictly in real time). Here, “promptly” means within, say, ~3 h, so as to permit data assimilation into model forecast update cycles. Additionally, both of these products must localize a storm spatially to within a reasonable scale of mesoscale-forecast variation, for example, 20 km.

To provide product (a), a VLF system must not miss significant storms within their 3-h evolution. Similarly, a VLF system must not falsely detect storms that do not in fact exist. To provide product (b), a VLF system must, even though its stroke DE is low, have a stroke DE that is statistically, but not strictly, proportional within a given meteorological regime (e.g., continental, maritime, island, etc.). If the DE were not statistically proportional, but instead varied randomly from storm to storm even in a fixed meteorological setting, then the detected lightning rate would provide no skill as a proxy for rainfall. If the DE were strictly proportional, then we could calibrate it. WWLLN seems to be better than unproportional, and worse than strictly proportional. An exemplary case (Chang et al. 2001) of lightning data assimilation where these requirements are met showed significant improvements in mesoscale-forecast skill. Similarly, recently it has been found that VLF long-range detection of lightning in remote, non-coastal Pacific maritime storms can be of use when assimilated into forecasts in that poorly covered region (Pessi et al. 2004). Both of these references provide background material on the utility, and also the limitations, of treating lightning stroke rates as a proxy for rainfall.

We will now test the ability of WWLLN to detect the same storms as detected by LASA, and to detect strokes at a rate that is statistically proportional to the...
strokes detected by LASA. We divide each day of our campaign into eight periods, each of 3-h duration, for the entire campaign from 27 April through 30 September. Next, the WWLLN and LASA lightning events are each put into a matrix of locations. The matrix pixel size is 0.2° x 0.2°, there are 1600 spatial pixels. (a) All LASA events, (b) all WWLLN events, (c) LASA CG events, and (d) LASA IC events. Each legend in (a)–(d) lists the max value of pixel occupancy, corresponding to the lightest shade at the top of the grayscale. In all boxes, the bottom of the grayscale (black) corresponds to zero occupancy.

Let \( N_L(j, k, m) \) be the 40 x 40 matrix for all LASA events, and let \( N_W(j, k, m) \) be the 40 x 40 matrix for all WWLLN events in 3-h epoch \( m \).

During each 3-h period, we tally three statistics:

1) the sum of the square of WWLLN pixel occupancy (proportional to autovariance):

\[
A_W = \sum_{j=1,40} \sum_{k=1,40} N_W^2(j, k, m)
\]

(Figure 7 shows an example of lightning-occurrence pixel maps during a single 3-h period on 13 August 2004. The various pixel-occupancy matrices are computed and stored for all 3-h epochs in the campaign.)

2) the sum of the square of LASA pixel occupancy (proportional to autovariance):
The larger-pixel case (Fig. 8b) has higher correlations than the smaller-pixel case (Fig. 8a).

Figure 8 indicates that WWLLN (despite its relatively low stroke-detection efficiency) detects storms with a high degree of spatial fidelity within a given 3-h epoch, based on the use of LASA as a benchmark. This is done despite the Florida stroke-detection rate for WWLLN being less than 1% overall of that for LASA (see Table 1). The evidence of Fig. 8 implies that WWLLN can provide useful lightning-location data for assimilation in model forecasts on a 3-h time scale.

The evidence of Fig. 8 addresses spatial fidelity of WWLLN data, compared to LASA. However, the question is not yet answered as to whether the WWLLN event counts are proportional, in a consistent way (over the many 3-h epochs), to the LASA event counts. We can make this argument about proportionality by considering not just proportionality within 3-h epochs (as done above in Fig. 8), but also overall proportionality over the entire 2004 cross-validation campaign. We take the entire campaign-summed total of each of the quantities defined in Eqs. (1)–(3), and then evaluate the campaign-global correlation

$$C_{\text{global}} = \frac{\sum \sum C_{LW_m}}{\sqrt{\left(\sum A_{L_m}\right) \times \left(\sum A_{W_m}\right)}}.$$  

(4)

We find that the global correlation so defined is 60.5%, indicating that WWLL over the course of an entire summer detects storms with stroke detections that are partially proportional to the stroke detections per storm by LASA. We find that a major part of the correlation’s departure from 100% is due to the averaging over all local times. To show this, we have broken this exercise into eight universal coordinated time bins, each 3 h long. Summing over all days in this study, the correlations for the eight 3-h periods are 65.6% (0000–0300 UTC), 68.9% (0300–0600 UTC), 75.4% (0600–0900 UTC), 62.6% (0900–1200 UTC), 72.6% (1200–1500 UTC), 67.8% (1500–1800 UTC), 68.7% (1800–2100 UTC), and 73.8% (2100–2400 UTC). Each of these time slices has a higher WWLLN/LASA internal proportionality than does the overall database (60.5%). This means that the efficiency of WWLLN in the Florida area varies with universal coordinated time.

Further work on this effect will be required before we can reduce this form of variability in WWLLN “calibration” in its estimates of lightning stroke rate.

8. Conclusions

The overall stroke-detection efficiency for WWLLN is less than 1%. However, strokes at higher current
amplitudes (>30 kA) are detected at ~4% efficiency. This is independent of the type and polarity of the stroke, and apparently depends only on stroke-current amplitude.

About half of the strokes LASA detects in Florida are ICs. WWLLN stroke detections in Florida are 26% IC. This indicates that WWLLN is able to detect storms that are dominantly IC, provided that some of the IC discharges are sufficiently high current.

WWLLN stroke detections, when they occur, are accurate to within 50 μs in time and 15–20 km in position. This spatial accuracy permits identification of the convective cell but not a finer-resolution analysis of the discharge position within the storm complex.

Despite its low overall stroke DE, and the steep selectivity of that DE for high-current amplitudes, WWLLN supplies a spatially accurate and representative census of storms on a 3-h averaging epoch. Moreover, the number of WWLLN strokes in these storms appears to be statistically proportional to the number of LASA strokes, though with as yet unmodeled local-time variations. When these variations are finally understood and modeled, then we expect that WWLLN will be able to furnish 3-h-update data assimilation (e.g., of latent-heat-release rate, or rain rate) into model forecasts, to the extent that one may prudently use lighting rate as a proxy for rain rate.

Acknowledgments. We are indebted to the entire LASA team for their kind cooperation. Two authors (ARJ and JH) were supported by the U.S. Department of Energy, under whose auspices the LASA array is operated. Two authors (RHH and EHL) were supported in part by a grant from the Mindlin Foundation. WWLLN data are provided through the University of Washington under agreement with Low Frequency Electromagnetics of New Zealand. ARJ was a visiting scholar at the University of Washington. We have profited from insightful suggestions by Craig Rodger.

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